

# Building the Material Flow Networks of Aluminum in the 2007 U.S. Economy

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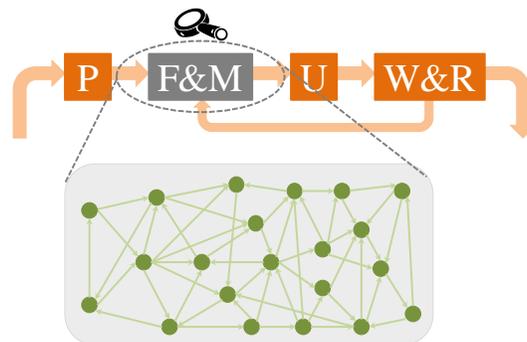
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17 **Abstract:** Based on the combination of the U.S. economic input-output table and the stocks and  
18 flows framework for characterizing anthropogenic metal cycles, this study presents a  
19 methodology for building material flow networks of bulk metals in the U.S. economy and applies  
20 it to aluminum. The results, which we term the Input-Output Material Flow Networks (IO-MFNs),  
21 achieve a complete picture of aluminum flow in the entire U.S. economy and for any chosen  
22 industrial sector (illustrated for the Automobile Manufacturing sector). The results are compared  
23 with information from our former study on U.S. aluminum stocks and flows to demonstrate the  
24 robustness and value of this new methodology. We find that the IO-MFN approach has the  
25 following advantages: (1) it helps to uncover the network of material flows in the manufacturing  
26 stage in the life cycle of metals; (2) it provides a method that may be less time-consuming but  
27 more complete and accurate in estimating new scrap generation, process loss, domestic final  
28 demand, and trade of final products of metals, than existing material flow analysis approaches;  
29 and, most importantly, (3) it enables the analysis of the material flows of metals in the U.S.  
30 economy from a network perspective, rather than merely that of a life cycle chain.

31 **Keywords:** material flow analysis, input-output analysis, complex network, industrial ecology

32

## 33 **1 Introduction**

34 An anthropogenic cycle is the quantitative characterization of the flows of a specific material into,  
35 within, and from a given anthropogenic system<sup>1</sup>, and is usually also reported as material flow  
36 analysis (MFA) or substance flow analysis (SFA). One of the most widely used methods of  
37 characterizing anthropogenic metal cycles is the Stocks and Flows framework developed by the  
38 Yale Center for Industrial Ecology<sup>1-5</sup>. In this approach, the life cycle of a metal in the  
39 anthroposphere is divided into four principal life stages - production, fabrication and  
40 manufacturing, use, and waste management & recycling, each of which can be further divided  
41 into several sub-stages when necessary and appropriate. By using statistics mainly released by  
42 industries, this framework has been applied to characterize the anthropogenic cycles of many  
43 metals<sup>4-12</sup>. However, a significant challenge of such studies is that in almost all cases existing  
44 statistics cannot enable researchers to characterize elemental flows within the manufacturing  
45 stage at a level that is sufficiently detailed to identify flow magnitudes among manufactured  
46 products. For example, U.S. aluminum statistics<sup>13</sup> (which are believed to be more detailed than  
47 those of other economies) can only support the characterization of aluminum flows from eight  
48 semi-fabricated products to seven general end-use sectors<sup>6</sup>, and there is a lack of data on  
49 aluminum flows (that are inferred to exist) among these seven end-use sectors.

50 Input-output analysis (IOA), a tool that has been widely used, provides monetary data on the  
51 inter-sectoral flows of goods and services within an anthropogenic system<sup>14</sup>. Compared to data  
52 that are from industrial statistics and are used in existing MFA/SFA studies to characterize metal  
53 flows in the manufacturing stage, data compiled in input-output (IO) tables have the great  
54 advantage that they are generally classified at quite high resolution. For example, the 2007 U.S.  
55 IO table includes 393 sectors, about 230 of which are categorized as manufacturing sectors<sup>15</sup>.

56 Another advantage is that the IO tables provide information on monetary flows among all these  
57 sectors, as well as monetary value added to, and final demand for, all these sectors.

58 These features of IO tables enable researchers to analyze monetary flows and material flows (if  
59 they can be generated from the monetary flows) at a very detailed level and as a network (rather  
60 than as a life cycle chain in existing MFA/SFA studies). However, challenges exist when  
61 attempting to convert monetary flows in IO tables into material flows: (1) data in IO tables are  
62 only compiled using monetary metrics; (2) flows in IO tables are for all economic activities rather  
63 than just for activities involving physical flows; namely, they also include flows resulting from  
64 services (e.g., education or consultation) that do not correspond to any physical flows among  
65 sectors; (3) physical flows in an economy comprise not only commodity flows (each sector  
66 produces at least its own commodity, and possibly commodities of other industries, according to  
67 the commodity-by-industry approach<sup>14, 15</sup>) but also flows of material scrap and flows of material  
68 losses into the environment. However, data in IO tables capture only the commodity flows among  
69 sectors while ignore the flows of material scrap and losses, or treat scrap flows of all materials as  
70 a whole to the Scrap sector rather than as separate scrap flows (e.g., separate aluminum scrap and  
71 iron scrap flows).

72 By using a price homogeneity assumption, Nakamura and colleagues developed the WIO-MFA  
73 (waste input-output MFA) model<sup>16, 17</sup> and the UPIOM (Unit Physical Input-Output by Materials)  
74 model<sup>18, 19</sup> that can be used to estimate iron and other metals flows among IO sectors in Japan.  
75 The WIO-MFA and UPIOM models help to address the challenges of converting IO monetary  
76 flows into physical flows for materials such as iron, aluminum, and plastics for which there are  
77 relevant independent sectors in the Japanese IO tables. This means that if one were to apply the  
78 WIO-MFA and UPIOM approaches to the U.S. IO tables, bulk metals including iron, aluminum,

79 and copper could be analyzed because U.S. IO tables have independent sectors for these three  
80 metals too. Thus, there is a significant potential to apply the WIO-MFA and UPIOM approaches  
81 in combination with existing MFA/SFA studies to characterize anthropogenic metal cycles at a  
82 highly detailed level in anthropogenic systems for which IO tables are available at fairly high  
83 resolution.

84 A further benefit of achieving detailed economy-wide characterization and quantification of  
85 material flows among sectors is that it creates a material-based version of an economic network  
86 that can be studied using complex network analysis (CNA) approaches<sup>20</sup>. CNA has been drawing  
87 increasing attention in the last two decades. However, few MFA/SFA studies have been analyzed  
88 using its tools. This is probably due to the fact that existing MFA/SFA studies supported by  
89 industrial statistics appear to be relatively simple systems. For example, there are typically less  
90 than twenty nodes in many MFA/SFA studies, and these studies are unable to explore inter-  
91 sectoral flows that would make the cycles look like a network rather than a life cycle chain.  
92 However, as mentioned above, if a MFA/SFA framework can be enhanced by transforming IO  
93 tables to provide a more detailed characterization of metal flows inside the manufacturing stage  
94 (meaning more nodes and inter-sectoral flows), it will be not only possible but also necessary to  
95 analyze the cycles using CNA tools and methods.

96 Thus, this study seeks to achieve the following goals using aluminum as the subject metal: 1)  
97 develop the method of building the IO-MFN (Input-Output Material Flow Network) for bulk  
98 metals in the entire U.S. economy, using data from a traditional MFA study<sup>6</sup> and the 2007 U.S.  
99 IO table<sup>15</sup>; 2) demonstrate how to build a detailed IO-MFN of the metal for specific IO sectors  
100 rather than for the entire U.S. economy, using the Automobile Manufacturing sector as an

101 example; and 3) compare results generated from this study with those from a traditional MFA  
102 study<sup>6</sup> to demonstrate the robustness and value of the IO-MFN approach.

## 103 **2 Methodology**

104 A network consists of two basic components: nodes and links between those nodes (also termed  
105 “edges” in network analysis parlance). The magnitudes of the edges are the “edge strengths”. In  
106 the IO-MFNs, the nodes correspond to economic sectors while the links represent the physical  
107 exchange of metal (e.g., embodied in products) between nodes. The nodes and links of the  
108 material flow network of aluminum in the U.S. economy can be roughly grouped into two  
109 categories: (1) those determined by using the 2007 U.S. IO table (Figure 1, in green); and (2)  
110 those determined based on a traditional MFA study<sup>6</sup> (Figure 1, in purple).

### 111 **2.1 Identifying Metal-Related Network Nodes**

112 A commodity-by-commodity (C×C) IO table in the 2007 U.S economy was first generated by  
113 using the “after redefinition make and use tables” that was compiled and released by the U.S  
114 Bureau of Economic Analysis (BEA)<sup>15</sup>. Within this monetary IO table, there are three regions: (I)  
115 the inter-sectoral flow region that depicts monetary transactions among sectors; (II) the value  
116 added region depicting the contribution of employees, business owners and capital, and  
117 government to each sector; and (III) the final demand region depicting the final demand for  
118 commodities of each sector by net export, domestic personal consumption, domestic private  
119 investment, domestic government purchases, and change in domestic private inventories (Table  
120 S1 in Supporting Information 01 (SI-01)).

121 Theoretically, if one were to build a network of monetary transaction flows, each sector in  
122 Region I, Region II, and Region III can be a node in this network. However, the present study

123 aims to build a material flow network of aluminum rather than one of monetary transactions, and  
124 wishes to make this network a harmonious part of the anthropogenic aluminum life cycle (Figure  
125 1). From this perspective, we take the following steps to identify and define nodes for our  
126 network:

127 **Step I:** Nodes corresponding to sectors (Region II) contributing non-physical value added to  
128 sectors in Region I are ignored, because there is no material flows embedded in these monetary  
129 value-added flows.

130 **Step II:** Nodes corresponding to sectors or sector groups receiving final demands from sectors or  
131 sector groups in Region I are divided into two categories (No. 13 and 14, Table S2 in SI-01):  
132 trade nodes and domestic final demand nodes. There is one trade node and one domestic final  
133 demand node corresponding to each sector or sector group, and each sector's domestic final  
134 demand node is the combination of that sector's domestic personal consumption, domestic  
135 private investment, domestic government purchases, and change in domestic private inventories.  
136 Because final goods of aluminum are generally grouped into end-use sectors, we identify 15 end-  
137 use sectors (Table S3 in SI-01) according to a guide prepared by the Aluminum Association<sup>21</sup>,  
138 and categorize all domestic final demand nodes into these 15 end-use nodes as appropriate.

139 **Step III:** Each sector in Region I is identified as a node, and all these 393 nodes are used to  
140 generate an inter-sectoral material flow network (Figure S1 in SI-01, excluding trade nodes and  
141 domestic final demand nodes). In order to make this network more tractable when visualizing  
142 them, sectors with similar features are grouped together when possible (Table S4 in SI-01). This  
143 simplification reduces the number of nodes from 393 to 99, each of which is given a label as  
144 demonstrated in Figure 3 and Table S4 in SI-01. For example, eleven vehicle component sectors

145 are combined to generate a node called Motor Vehicle Parts, and twenty-four food sectors are  
146 combined to generate a node called Foods. These 99 nodes are then classified into 12 categories  
147 (No. 1-12, Table S2 in SI-01; Table S4 in SI-01) and are distributed in Figure 3 from left to right  
148 roughly according to their progression along the stages of manufacturing.

149 **Step IV:** Nine external nodes that are not based on the IO table (the purple nodes in Figure 1) are  
150 identified so that the whole anthropogenic aluminum life cycle can be included. Most of these are  
151 self-explanatory, but a few deserve comment. One issue is that the mining of bauxite is found  
152 together with several other minerals in the “Other Nonmetallic Minerals Mining and Quarrying”  
153 sector, while the production of alumina and the refining of alumina to produce aluminum are  
154 aggregated into a single sector in the IO tables, but these three steps can be distinguished on the  
155 basis of MFA information. Similarly, the transaction of aluminum scrap may be recorded in the  
156 flows from each sector to the Scrap sector, but these flows include scrap for all materials, making  
157 it impossible to estimate aluminum scrap flows using just the IO table data. Finally, loss and in-  
158 use stock of aluminum are not captured by IO tables so it is necessary to add an external node for  
159 each of them.

## 160 2.2 Determining Links to Connect Nodes

161 The links determined by using the 2007 IO table (Figure 1, in green) can be classified into five  
162 types: (1) aluminum flows among sectors; (2) aluminum contained in traded commodities; (3)  
163 domestic final demand of aluminum contained in domestically used commodities; (4) new  
164 aluminum scrap generated from each sector; and (5) aluminum loss from each sector. Note that  
165 data on these links are first estimated for each of the 393 sectors, and data on links for the 99  
166 sector groups are then calculated for visualization in Figure 3. Links that are known to be relevant  
167 but which cannot be determined by using the 2007 IO table (Figure 1 in purple) can be classified

168 into two types: (1) links introducing aluminum into the inter-sectoral network; and (2) links used  
169 for closing the aluminum life cycle. The following steps describe details of determining data for  
170 these links.

171 **Step I:** Aluminum metal is introduced into the inter-sectoral network from three sources –  
172 domestic primary aluminum production, domestic secondary aluminum production, and net  
173 import of unwrought aluminum. The first of these requires special treatment because there is no  
174 IO sector specifically for bauxite mining, while alumina refining and primary aluminum smelting  
175 are integrated into one sector in the 2007 U.S. IO table. To address this issue, aluminum flows  
176 from bauxite mining to alumina refining and then to primary aluminum smelting compiled by a  
177 relevant MFA study<sup>6</sup> are used to introduce domestically-produced primary aluminum (2.5 million  
178 metric tons (MMTs)) into the network. We then create two external nodes, New Scrap and Old  
179 Scrap Preparation, to introduce both new and old scrap into the IO sector Secondary Smelting  
180 and Alloying of Aluminum (SSAA) that represents the production of secondary aluminum. The  
181 production of secondary aluminum from new and old scrap<sup>6</sup> is then used to introduce  
182 domestically-produced secondary aluminum (3.6 MMTs) from sector SSFA to the sector  
183 Aluminum Refining and Primary Aluminum Production (AR&PAP). Note that secondary  
184 aluminum is introduced into the network through the AR&PAP node because in the 2007 IO  
185 table all output of SSAA sector is reported to be sold to the AR&PAP sector. This means that the  
186 use of primary and secondary aluminum by the U.S. economy is reported together in the IO table  
187 rather than individually. Finally, U.S. net import of unwrought aluminum (2.6 MMTs), compiled  
188 by the relevant MFA study<sup>6</sup>, is also introduced into the network through the node AR&PAP. The  
189 total of aluminum metal introduced into the U.S. economy in 2007 then becomes 8.7 MMTs.

190 **Step II:** Aluminum metal introduced into the inter-sectoral network is spread across the whole  
 191 network node by node, starting from the AR&PAP node, according to the monetary distribution  
 192 ratios recorded in the IO table. All monetary transactions are classified into five categories as  
 193 demonstrated in Figure 2. Only when the monetary flows from a node (e.g., node a in Figure 2)  
 194 belong to category I are the monetary IO values used to distribute aluminum to subsequent nodes.  
 195 Otherwise, if monetary flows are from nodes of types d, e, and f (meaning flows belong to  
 196 categories II, III, or IV), then no aluminum flows occur from one IO sector to another. In addition,  
 197 we exclude all self-loop transaction flows (category V) because a sector does not use itself as a  
 198 component. A binary matrix  $\Phi$  (in which the element is 1 when the corresponding IO table's  
 199 monetary transaction belongs to category I; otherwise the matrix element is 0) is then generated  
 200 (Supporting Information 02 (SI-02)). Because new scrap is formed and metal loss occurs in every  
 201 sector that processes aluminum or aluminum-containing products, a new scrap ratio matrix  
 202  $R^S$  and a loss ratio matrix  $R^L$  are also generated (Details are described in Section S2.2. of SI-01;  
 203 the two matrices are provided in SI-02).

204 The monetary direct requirement coefficient matrix  $A$  is partitioned and reorganized as follows:

$$205 \quad A = \begin{pmatrix} A_{MM} & A_{MP} \\ A_{PM} & A_{PP} \end{pmatrix} \quad (1)$$

206 where M indicates the studied material that is aluminum in this paper, P indicates products that  
 207 include all other 392 sectors,  $A_{MP}$  is a  $1 \times 392$  vector that represents the monetary distribution of  
 208 aluminum from AR&PAP to all other sectors, and  $A_{PP}$  is a  $392 \times 392$  matrix. The matrixes  $\Phi$ ,  $R^S$ ,  
 209 and  $R^L$  are partitioned and reorganized similarly.

210 A matrix that represents the distribution of aluminum among all sectors ( $\tilde{A}_{PP}$ ) is then generated  
 211 by the following equation:

$$212 \quad \tilde{A}_{PP} = \Gamma_{PP} \otimes \Phi_{PP} \otimes A_{PP} \quad (2)$$

213 where  $\otimes$  indicates the Hadamard product (the element wise product of two matrices).  $\Gamma_{PP}$  is the  
 214 yield ratio matrix, which is given by:

$$215 \quad \Gamma_{PP} = I - R_{PP}^S - R_{PP}^L \quad (3)$$

216 A  $1 \times 392$  vector,  $C_{MP}$ , which represents the aluminum content in all sectors is then derived by  
 217 formula (4)<sup>18</sup>:

$$218 \quad C_{MP} = \tilde{A}_{MP} (I - \tilde{A}_{PP})^{-1} \quad (4)$$

219 where  $\tilde{A}_{MP}$  represents the physical input coefficient of aluminum to other commodities and is  
 220 given by

$$221 \quad \tilde{A}_{MP} = \frac{T_{Al}}{D_{Al}^{Int} + D_{Al}^{Fnl}} \cdot \Gamma_{MP} \otimes A_{MP} \quad (5)$$

222 where  $T_{Al}$  represents the metric tons of aluminum used by the entire U.S. economy in 2007 (i.e.  
 223  $T_{Al}=8.7$  MMTs),  $D_{Al}^{Int}$  and  $D_{Al}^{Fnl}$  are the monetary intermediate use and the monetary domestic  
 224 final demand of AR&PAP in the 2007 U.S. economy, respectively.  $\Gamma_{MP}$  is the yield ratio vector  
 225 from AR&PAP to all other sectors, and is given by  $I - R_{MP}^S - R_{MP}^L$ .

226 A matrix  $U_{Al}$  representing the flows of aluminum among sectors then becomes:

$$227 \quad U_{Al} = \begin{pmatrix} \text{diag}(C_{MP})\tilde{A}_{PP} \\ \tilde{A}_{MP} \end{pmatrix} \text{diag}(((I - \tilde{A}_{PP})^{-1})f_P) \quad (6)$$

228 where  $f_p$  is the monetary final demand of all other 392 sectors in the 2007 U.S. economy.  $(U_{Al})_{i,j}$   
 229 represents the amount of aluminum sent from sector  $i$  to sector  $j$ , which will then be incorporated  
 230 into the body of sector  $j$ .

231 **Step III:** Aluminum metal leaves the inter-sectoral network in four ways: (1) process loss and (2)  
 232 new scrap generation occurring in each sector, and (3) net export and (4) domestic final demand  
 233 of commodities generated by each sector. The loss and new scrap generation occurring in sector  
 234  $j$  are estimated by:

$$235 \quad L_j = R_j^L \cdot \sum_i (U_{Al})_{i,j} \quad (7)$$

$$236 \quad S_j = R_j^S \cdot \sum_i (U_{Al})_{i,j} \quad (8)$$

237 The aluminum embedded in final demand  $k$  for sector  $j$  is given by:

$$238 \quad F_j^k = C_{MPj} f_{Pj}^k \quad (9)$$

239 Then the five types of final demand are integrated into two groups: net export (import + export)  
 240 and domestic final demand (personal consumption + private investment + government + change  
 241 in private inventories).

242 **Step IV:** The life cycle of aluminum is closed by adding nodes for the in-use stocks, for the old  
 243 scrap collection and preparation, and for the unidentified end-of-life aluminum (landfilled,  
 244 exported as end-of-life products, or hibernating). From the life cycle perspective, the challenge of  
 245 the inter-sectoral network built by this study is that it ends at the step where aluminum enters the  
 246 in-use stock. Were similar studies to be done for a long-enough period before 2007, the historical  
 247 flows of aluminum entering the in-use stock could be estimated sector by sector, and the

248 historical sector-level end-of-life flows of aluminum from in-use stock could also be modeled  
249 using the dynamic lifespan modeling method<sup>22, 23</sup>. However, because only the 2007 analysis has  
250 been done to this point, we use data from a former study<sup>6</sup> in which the old scrap flows were  
251 provided as a sum of all commodities rather than sector by sector.

### 252 **2.3 Building Sub-Networks for Sectors**

253 The inter-sectoral network for which the data are generated by equation (6) represents the  
254 aluminum flow network for the entire U.S. economy. However, it is straightforward to generate  
255 data for sub-networks for either a certain sector or a certain group of sectors by replacing  $f_p$  in  
256 equation (6) by  $f_{P_n}$  or  $f_{P_g}$ , respectively, where  $f_{P_n}$  represents the final demand of a certain sector  
257  $n$  and  $f_{P_g}$  represents the final demand of a certain group of sectors.

### 258 **2.4 Validating the Approach**

259 The validation of the IO-MFN approach was conducted by two methods: (1) by checking whether  
260 mass balance is achieved for each node and for the entire inter-sectoral network, and (2) by  
261 comparing data generated from this study with data that already exist or that were generated from  
262 a former study<sup>6</sup>. The comparison was done for the following four groups: (1) the MFA-based  
263 physical data for alumina and aluminum were multiplied by their prices to generate monetary  
264 data, which were then compared with the corresponding monetary data that already exist in the  
265 IO table (details in Table S6 in SI-01); (2) for the 15 end-use sectors (Table S3 in SI-01) that  
266 were further classified into seven end-use sectors identical to those used by the Aluminum  
267 Association<sup>21</sup>, a new set of data on aluminum shipments to domestic markets by end-use sector  
268 (details in Section S4 in SI-01) was generated and compared with those estimated by the  
269 Aluminum Association<sup>13</sup>; (3) the modeled aluminum trade embedded in final products was  
270 grouped into the seven end-use sectors and compared with those estimated using physical data in

271 our former study<sup>6</sup>; and finally, (4) the modeled new scrap generation from all sectors was totaled  
272 and then compared with statistics on new scrap use provided by the Aluminum Association<sup>13</sup>.

## 273 **2.5 Visualizing the Material Flow Networks**

274 With all nodes and data for links among nodes determined, the material flow networks of  
275 aluminum were visualized using the open source software Gephi<sup>24</sup>. We did so for both (1) the  
276 network covering the whole economy and (2) the network for domestically producing  
277 automobiles in the United States (by assuming final demands for all other sectors are zero). For  
278 the automobile network, only the inter-sectoral nodes are shown (i.e., excluding those nodes and  
279 links for introducing aluminum into the network and for closing the life cycle) and nodes not  
280 connected to the automobile network are deleted (Figure S3 in SI-01).

## 281 **3 Results**

282 Figure 3 presents the material flow network of aluminum in the entire 2007 U.S. economy. It  
283 traces the flow of aluminum from alumina and scrap input through to final demands (divided into  
284 net export and domestic final demand), process loss, and new scrap generation. The life cycle is  
285 closed by using the in-use stock to link domestic final demands with old scrap collection and  
286 preparation. The width of each link in the network diagram is proportional to the material flow  
287 strength of aluminum along that link. (Note that the 393 sectors in the original input-output table  
288 have been categorized into 99 sector groups, and only these 99 nodes are shown in Figure 3 (Step  
289 III in section 2.1). Mass balance (input equals output) is achieved for each of the 393 sectors and  
290 the 99 sector groups, and for the whole of the 393 sectors in Region I. Two figures illustrating the  
291 inter-sectoral flows among the 393 sectors in Region I either as a network or as a 3-D matrix are  
292 provided in SI-01 (Figures S1 and S2). A comprehensive analysis of this inter-sectoral network is  
293 performed in a companion paper<sup>20</sup>.

294 Using the Automobile Manufacturing sector as an example, [Figure 4](#) demonstrates the material  
295 flow network of aluminum for domestically producing automobiles in the United States in 2007.  
296 It clearly shows the sectors that play roles in introducing aluminum step by step into automobiles,  
297 as well as the contribution of each sector to the network. Similar networks can be derived for  
298 other sectors as desired, such as Aircraft Manufacturing, Computer Manufacturing, Light Truck  
299 and Utility Vehicle Manufacturing, and so on.

300 A comparison between the monetary data compiled by the IO table and the monetary data  
301 estimated using the physical and price data for the sum of aluminum introduced into the inter-  
302 sectoral network shows that the difference between these two sets of data is less than 10% ([Table](#)  
303 [S6 in the SI](#)). Given the effects of price fluctuations, we regard this difference as reasonable, and  
304 regard the amount of aluminum (which is 8.7 MMTs) introduced into the network as reflecting  
305 the actual use of aluminum in the entire 2007 U.S. economy. [Figure S4 in SI-01](#) demonstrates  
306 that the results estimated by this study are similar to the corresponding information provided by  
307 the Aluminum Association or estimated by our former MFA study. The total new scrap  
308 generation modeled by the current work is about 2.2 MMTs of aluminum metal, only about 5%  
309 less than the metal recovery from new scrap reported by the Aluminum Association (2.3  
310 MMTs)<sup>13</sup>. These comparisons help to further certify the robustness and reliability of the IO-MFN  
311 approach.

## 312 **4 Discussion**

313 By taking advantage of the combination of the U.S. economic input-output table and of physical  
314 data from an analogous MFA study, this paper uses aluminum as an example for a methodology  
315 of building material flow networks for bulk metals (iron, aluminum, and copper) in the U.S.  
316 economy. This methodology consists of two important aspects: (1) identifying nodes for the IO-

317 MFNs for metals; the whole collection of nodes represents the entire U.S. economy in which  
318 metals flow among sectors and all nodes are exclusive of one another; and (2) identifying the  
319 existence of links among nodes and determining data for these links. Using completely the same  
320 methodology and similar physical data, the IO-MFN for iron and copper in the 2007 U.S.  
321 economy can readily be built because the IO table has distinct sectors for those metals as well as  
322 for aluminum. The IO-MFN can also be built for other metals by additional manipulations and  
323 assumptions as reported in another companion paper<sup>25</sup>. A particular feature of this methodology  
324 is that IO-MFNs for only a single sector or a group of sectors can be built. If input-output tables  
325 in other economies are as detailed as that in the United States (e.g., Japan<sup>26</sup>), similar studies can  
326 be done for those economies.

327 Existing MFA studies for metals rely on information on the shipments of metal to the domestic  
328 market (reported as apparent consumption) by end-use sector to determine flows in the  
329 manufacturing and use stages, and the in-use stocks. However, there are several limitations for  
330 this end-use sector information: (1) the information is only for aggregated end-use sectors such as  
331 transportation or consumer durables rather than for specific products such as automobiles or  
332 refrigerators<sup>23</sup>; (2) the methods of classifying end-use sectors are material-specific and are  
333 generally inconsistent among metals; (3) for sectors that include many heterogeneous products, it  
334 is difficult to estimate a reasonable average product lifespan, therefore resulting in high  
335 uncertainties in estimation of in-use stocks; and (4) no information on flows among end-use  
336 sectors and especially among specific products, such as the use of electronics by automobiles, is  
337 reported. Because the U.S. input-output table enables us to analyze the aluminum flows among  
338 almost 400 sectors in this approach, these four limitations can be readily addressed by the  
339 approach developed in this study.

340 The IO-MFN approach helps to uncover the networks of material flows in the manufacturing  
341 stage of the life cycle of metals. It also enables us to estimate and visualize the new scrap  
342 generation and material loss of metals from each sector. (In contrast, the Aluminum Association  
343 reports only the new scrap generation of aluminum as a whole<sup>13</sup>). With the information on  
344 aluminum flows that is reported as part of final demands in the U.S. economy, the approach helps  
345 estimate the trade of aluminum contained in all kinds of final products. Compared to the MFA  
346 method using physical data from the UN Comtrade database and its respective aluminum content  
347 information<sup>6</sup>, the present work provides a solution that is much less time-consuming and arguably  
348 more complete and accurate. Note from [Figure S4\(b\) in SI-01](#) that this study provides results on  
349 the trade of aluminum contained in products in sectors such as Containers & Packaging and  
350 Others, which we found almost impossible to estimate using physical data. The final (and  
351 probably the most important) advantage of this approach is that it enables us to analyze the  
352 material flows of metals in the U.S. economy as a network, rather than merely a life cycle chain,  
353 so that we can draw on the indicators developed by complex network science to analyze the  
354 supply risk, the impacts of supply risk, and the criticality of metals<sup>20</sup>.

355 There are several limitations to this approach that originate from either the limitations of the U.S.  
356 input-output data or from assumptions that are made when building the IO-MFNs. Because the  
357 U.S. input-output tables at the  $\approx 400$ -sector level are compiled only at five year intervals (the most  
358 recent version is for 2007), the material flow networks can be made for only these years. This  
359 results in the challenge of lacking both annual and up-to-date information. In addition, the  
360 classification of the IO sectors was slightly changed from version to version of the IO tables.  
361 Therefore, if one were to apply the approach to derive historical input and output flows of the in-  
362 use stocks and to estimate the in-use stocks at the IO-sector level, suitable assumptions and

363 adjustments of the data have to be made so that consecutive annual information for historically  
364 consistent sectors can be derived.

365 The process of building the IO-MFNs is not perfect, and is thus subject to further improvement.  
366 There are two types of assumptions that may result in challenges: (1) the values of elements in  
367 the matrixes  $\Phi$ ,  $R^S$ , and  $R^L$  are determined by the combination of data from various references  
368 and expert judgment; and (2) the distribution of aluminum from one node to those other nodes  
369 that purchase products from it is determined according to the distribution of monetary values  
370 among nodes, meaning that we apply the price homogeneity assumption as described in  
371 references<sup>18, 27</sup>. This assumption implies that every dollar of products sold from a particular IO  
372 sector contains the same amount of the studied metal, which may or may not be true (products  
373 sold to Scrap do not apply this assumption). Thus, if the aluminum content per dollar of products  
374 sold from one node to other nodes is heterogeneous, a skewed metal branching ratio will result,  
375 as illustrated in [Figure S5 in SI-01](#). A possible solution for addressing this challenge resulting  
376 from the price homogeneity assumption is to get information on the price heterogeneity for each  
377 node, and to then generate a corresponding matrix  $H$  for adjusting the difference. However,  
378 getting the price heterogeneity information can be very time-consuming (or even impossible).

379 This challenge raises the question “What is represented by the numbers in the derived IO matrix,  
380  $U_{Al}$ , for the IO-MFN?”. In a traditional IO table the entries in each matrix element are the  
381 aggregated transactions between sectors of the economy, and are denominated in monetary units  
382 (dollars in the case of the U.S. IO table). In a derived IO matrix for IO-MFN, in contrast, the  
383 entries represent amounts of metal that are transferred from one sector of the economy to another.  
384 However, the correspondence between monetary units and metal units is not equivalent across the  
385 IO table, because monetary transactions in the metal IO table generally involve other metals and

386 assemblages of the material as well. At the early stages of the aluminum cycle, the flows from the  
387 AR&PAP sector to initial customers are closely related to the amount of metal exchanging  
388 ownership. Subsequent transactions are less and less closely related to the pure metal for which  
389 the table was constructed, however, and are more accurately regarded as reflections of the metal-  
390 related value of the increasingly complex assemblages that are involved in product manufacturing  
391 processes. In place of the common but (in this case) inaccurate unit of metric tons, we term the  
392 aggregated quantities in the elements of a derived IO matrix for IO-MFN as “transformed metal  
393 unit (TMU)”, and denominate them in “hektes”. These are terms that parallel the economist’s  
394 monetary units of dollars or yen. (The hekte, pronounced “hecktuh”, is thought to have been the  
395 first metal coinage, used in Lydia [now Western Turkey] in the 7<sup>th</sup> century BPE<sup>28</sup>. The use of  
396 TMU and hektes remind us that TMU can be denominated, but not strictly in unit of either metric  
397 tons or dollars.

398 The methodology described above is able to generate a metal-based IO table from an economic  
399 IO table provided that a material flow analysis is available to supply nodes that are important to  
400 quantifying those ensemble metal flows that are extraneous to the economic IO table. Despite its  
401 limitations, we believe that the approach has been validated with satisfactory robustness and  
402 reliability. And, as suggested here but demonstrated more completely in two subsequent papers<sup>20</sup>,  
403 <sup>25</sup>, the result meets all requirements to be regarded as a network. The network can then be  
404 analyzed by the tools of CNA<sup>20</sup> and similar networks for other metals can be built<sup>25</sup>. Accordingly,  
405 we term this methodology the IO-MFN approach to emphasize the integration of MFA, IOA, and  
406 CNA.

407

408 **Supporting Information**

409 Details on methodology, data compilation, and complementary figures are listed. This material is  
410 available free of charge via the Internet at <http://pubs.acs.org>.

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414 **Notes**

415 The authors declare no competing financial interest.

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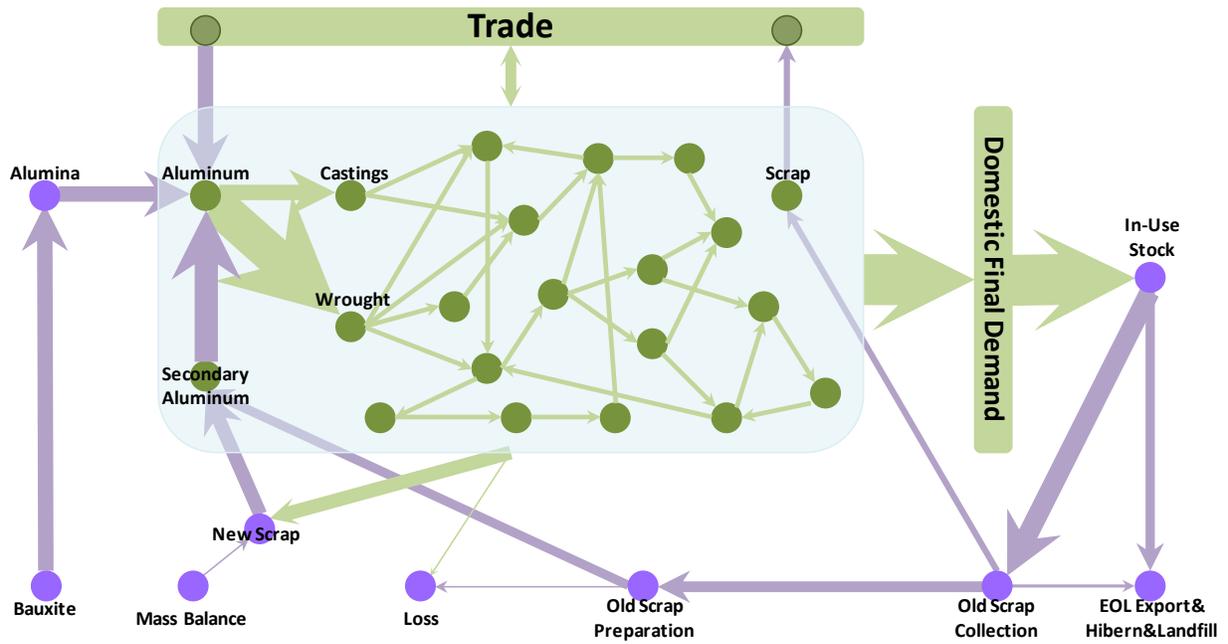
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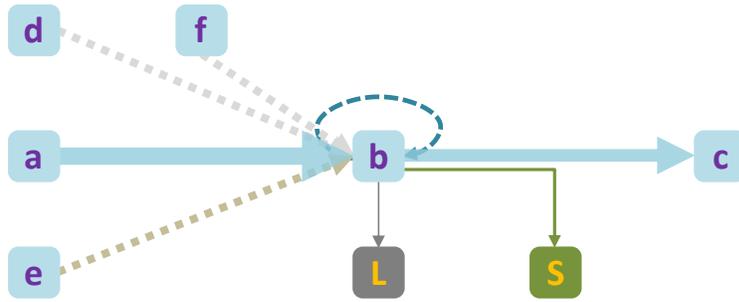
486 **Figures**



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 488 Figure 1 Schematic diagram demonstrating the embeddedness of the inter-sectoral material flow  
 489 network of aluminum in the anthropogenic aluminum life cycle. Green nodes and links are  
 490 determined using the U.S. input-output table (nodes for trade and domestic final demands are not  
 491 shown), while purple nodes and links are determined based on a traditional MFA study<sup>6</sup> so as to  
 492 demonstrate the whole aluminum life cycle.

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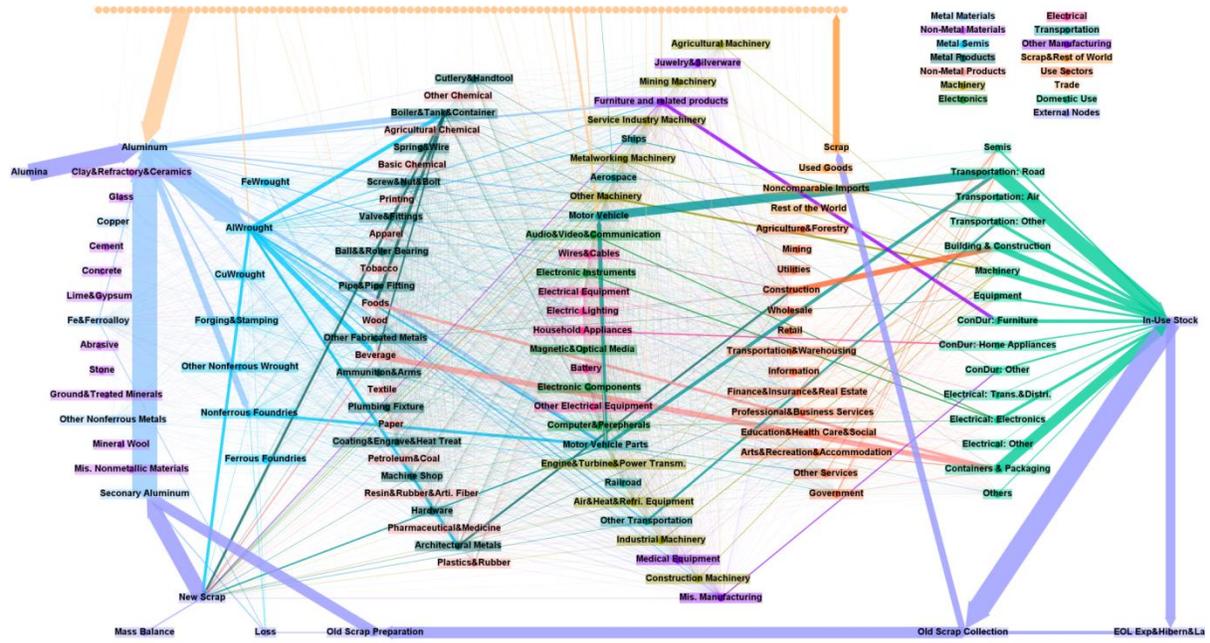
Category	Flows	Flows Description
I	a-b, b-c	Physical flows with aluminum that will be integrated into commodities of sectors b and c, respectively
II	e-b	Monetary flow without physical flow
III	d-b	Physical flow without aluminum in it
IV	f-b	Physical flow with aluminum that is not integrated into commodities of sector b
V	b-b loop	Flow from an sector to itself
Loss	b-L	Aluminum loss from sector b
New Scrap	b-S	New scrap generated from sector b

498 Figure 2 Schematic diagram illustrating the heterogeneities of inter-sectoral flows of input-output  
 499 tables when converting monetary flows into material flows of aluminum, as well as the loss and  
 500 new scrap flows that are not captured by input-output tables. Each of the letters a-f represents a  
 501 sector in the input-output table, while L and S indicate loss and new scrap, respectively.

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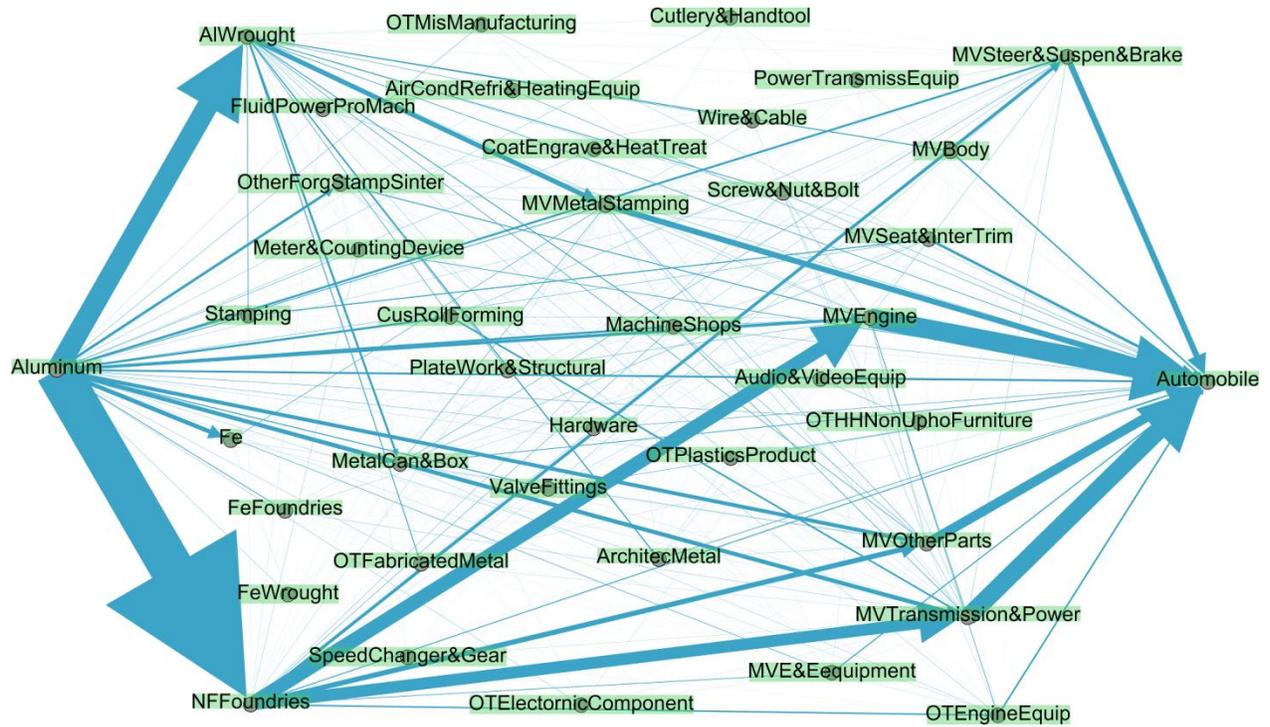
506 Figure 3 Material flow network of aluminum in the entire 2007 U.S. economy. The flow from  
 507 bauxite to alumina is not shown for simplicity. Refer to Tables S2-S5 in the Supporting  
 508 Information for the exact meaning of each node.

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514 Figure 4 Material flow network of aluminum for producing automobiles in the United States in  
515 2007. Refer to Tables S2-S5 in the Supporting Information for the exact meaning of each node.

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